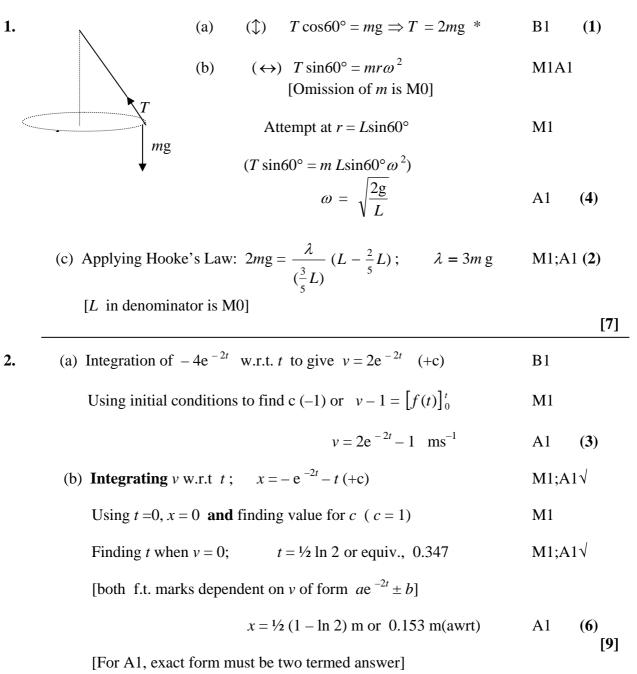
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PMT

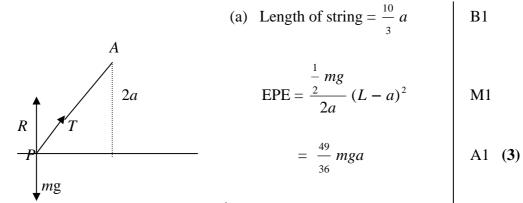
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PMT

[10]

3. (a) $F = \frac{k}{k^2}$ [k may be seen as Gm_1m_2 , for example] M1 Equating F to mg at $\mathbf{x} = \mathbf{R}$, $[mg = \frac{k}{R^2}]$ **M**1 Convincing completion $[k = mgR^2]$ to give $F = \frac{mgR^2}{r^2} *$ A1 (3) [Note: *r* may be used instead of *x* throughout, then $r \rightarrow x$ at end.] Equation of motion: $(m)a = (-) \frac{(m)gR^2}{r^2}$; $(m)v\frac{dv}{dr} = -\frac{(m)gR^2}{r^2}$ (b) M1;M1 $\frac{1}{2}v^2 = \frac{gR^2}{r}$ (+ c) or equivalent Integrating: M1A1 [S.C: Allow A1 $\sqrt{}$ if A0 earlier due to "+" only] Use of $v^2 = \frac{3gR}{2}$, x = R to find $c [c = -\frac{1}{4}gR]$ or use in def. int. **M**1 $\left[v^2 = \frac{2gR^2}{r} - \frac{gR}{2}\right]$ [Using x = 0 is M0] Substituting x = 3R and finding V; $V = \sqrt{\frac{gR}{c}}$ M1;A1 (7) [Using x = 2R is M0] *Alternative in (b)* Work/energy (-) $\int_{-\infty}^{a} \frac{mgR^{2}}{r^{2}} dx$; = $\frac{1}{2}mv^{2} - \frac{1}{2}mu^{2}$ M1;M1 $\left[\frac{mgR^{2}}{r} - \frac{mgR^{2}}{R}\right] = \frac{1}{2}mv^{2} - \frac{1}{2}m\frac{3gR}{2}$ Integrating: M1A1M1 M1A1 Final 2 marks as scheme [Conservation of energy scores 0]

4.



(b) Energy equation:
$$\frac{1}{2}mv^2 + \frac{\frac{1}{2}mg}{2a}a^2 = (\frac{49}{36}mga)_C$$
 M1A13

$$v = \frac{2}{3} \sqrt{5ga}$$
 or equivalent A1 (3)

(c) When string at angle
$$\theta$$
 to horizontal, length of string $= \frac{2a}{\sin \theta}$
 \Rightarrow Vert. Comp. of T , $T_{V} = T \sin \theta = \frac{mg}{2a} (\frac{2a}{\sin \theta} - a) \sin \theta$
 $= \frac{mg}{2} (2 - \sin \theta)$
(1) $R + T_V = mg$ and find $R =$ M1

$$\mathbf{R} = m\mathbf{g} - \frac{mg}{2}(2 - \sin\theta) = \frac{mg}{2}\sin\theta \qquad A1$$

$$\Rightarrow R > 0$$
 (as $\sin \theta > 0$), so stays on table A1 (5)

[Alternative final 3 marks: As
$$\theta$$
 increases so T_V decreases M1
Initial T_V (string at β to hor.) = $\frac{7}{10}mg$ A1
 $\Rightarrow T_V \le \frac{7}{10}mg < mg$, so stays on table A1] [11]

5.

(a) R $\frac{\lambda = 48N}{BA_0 = 0.9 \text{ m}}$ → A → 0.2g -0.6m Applying Hooke's Law correctly : e.g. $T = \frac{48x}{0.6}$ **M**1 Equation of motion: (-) $T = 0.2 \ddot{x}$ M1 Correct equation of motion: e.g. $-\frac{48x}{0.6} = 0.2 \ddot{x}$ A1 Writing in form $\ddot{x} = -\omega^2 x$, and stating motion is SHM A1√ Period = $\frac{2\pi}{\omega} = \frac{2\pi}{20} = \frac{\pi}{10}$ * (no incorrect working seen) A1 (5) [If measure x from B or A, final 2 marks only available if equation of motion is reduced to $\ddot{X} = -\omega^2 X$] (b) max v = aw with values substituted; $= 0.3 \times 20 = 6 \text{ ms}^{-1}$ M1A1(2) (c) Using $x = 0.3\cos 20t$ or $x = 0.3\sin 20T$ **M**1 Using x = 0.15 to give either $\cos 20t = \frac{1}{2}$ or $\sin 20T = \frac{1}{2}$ **M**1 Either $t = \frac{\pi}{60}, \frac{5\pi}{60}$ or $T = \frac{\pi}{120}$ A1 Complete method for time: $t_2 - t_1$, or $\frac{\pi}{10} - 2t_1$, or $2(\frac{\pi}{40} + T)$ **M**1 Time = $\frac{\pi}{15}$ s (must be in terms of π) A1 (5) [12]

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6. (a) Cylinder Hemisphere S $(\rho)\pi(2a)^2(\frac{3}{2}a)$ $(\rho)\frac{2}{3}\pi a^3$ $(\rho)(\frac{16}{3}\pi a^3)$ Masses M1A1 $[6\pi a^3]$ [18] [2] [16] $\frac{3}{2}a$ \overline{x} $\frac{1}{8} a$ Distance of B1B1 CM from O Moments equation: $6\pi a^3(\sqrt[3]{4}a) - \frac{2}{3}\pi a^3(\frac{3}{8}a) = \frac{16}{3}\pi a^3 \bar{x}$ M1 $\overline{x} = \frac{51}{64}a$ A1 (6) (b) G above "A" seen or implied **M**1 or $mg \sin \alpha (GX) = mg \cos \alpha (AX)$ α $\tan \alpha = \frac{AX}{XG} = \frac{2a}{\frac{3}{2}a - \bar{x}}$ A **M**1 ά $[GX = \frac{3}{2}a - \frac{51}{64}a = \frac{45}{64}a, \tan \alpha = \frac{128}{45}] \qquad \alpha = 70.6^{\circ}$ A1 (3) (c) Finding F and R : $R = mg \cos \beta$, $F = mg \sin \beta$ **M**1 Using $F = \mu R$ and finding $\tan \beta$ [= 0.8] **M**1 $\beta = 38.7^{\circ}$ A1 (3)

[12]

(a) Energy: $\frac{1}{2}mv^2 - \frac{1}{2}mu^2 = mga\sin\theta$ M1 $v^2 = \frac{3}{2}ga + 2ga\sin\theta$ A1 (2)(b) Radial equation: $T - mg\sin\theta = m\frac{v^2}{a}$ M1A1 $T = \frac{3mg}{2}(1 + 2\sin\theta)$ any form A1☆ (3) (c) Setting T = 0 and solving trig. equation; $(\sin \theta = -\frac{1}{2}) \Rightarrow \theta = 210^{\circ} *$ M1;A1(2) (d) Setting v = 0 in (a) and solving for θ M1 $\sin\theta = -\frac{3}{4}$ so not complete circle A1 (2) OR Substituting $\theta = 270^{\circ}$ in (a); $v^2 < 0$ so not possible to complete (e) No change in PE \Rightarrow no change in KE (Cof E) so v = u**B**1 (1) (f) When string becomes slack, $V^2 = \frac{1}{2} ga [\sin \theta = -\frac{1}{2} in (a)]$ B1☆ Using fact that horizontal component of velocity is unchanged M1 $\sqrt{\frac{ga}{2}} \cos 60^\circ = \sqrt{\frac{3ga}{2}} \cos \phi$ $\cos\phi = \sqrt{\frac{1}{12}} \Rightarrow \phi = 73.2^{\circ}$ M1A1 (4) [14]

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7.